## Logical Languages part 3 <br> 2020

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## Prolog

To access the lab computers, ssh into johnston and then ssh into one of the host computers in the lab. To see what hosts are available type in the johnston command line cat ~irina/hostnames

There are a couple of files available for download from the class website, such as simple.pl.

## Prolog

:- implies symbol
, and symbol

- Right side implies left side Right side can have and
- Headless or headed
- Facts

Rules
Goals/Queries

- Variables: start with capital letter


## Prolog

## Prolog demos

simple.pl file includes:
\% Simple example for testing
\% swipl from command line
\% Inside compiler:
\% ['simple.pl'].
\% person(bob).
\% returns true
\% father(bob,X).
\% returns $X=$ sam.
\% control d to exit
person(bob).
father(bob,sam).

## Prolog

## Prolog demos

simple.pl let's try it in compiler:
> swipl from command line
> Inside compiler:
['simple.pl'].
> control d to exit

Notice we always have a period after statement

## Prolog

## Prolog demos

simple.pl let's try it in compiler:
> swipl from command line
> Inside compiler:
['simple.pl'].
Things to try:
person(bob). father(bob,X).

## Prolog

## Prolog demos

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> swipl from command line
> Inside compiler:
['simple.pl'].
Things to try:
person(bob). Returns true
father(bob,X). Returns X=sam

## Prolog

## Prolog demos

simplemore.pl let's add more facts to file:
person(bob).
father(bob,sam).
father(sam,liz).
father(bob,X).
Returns?

## Prolog

## Prolog demos

simplemore.pl let's add more facts to file:
person(bob).
father(bob,sam).
father(sam,liz).
father(bob,X).
Returns?
initially returns $\mathrm{X}=$ sam
Type; and will return next item here:
X = liz

## Prolog

## Prolog demos

Let's try simple2.pl
\%http://faculty.otterbein.edu/psanderson/csc326/notes/PrologNotes.html
mother(iva, pete). mother(iva, ed). mother(iva, becky). mother(kay, nancy). mother(kay, bob). mother(kay, diane). mother(becky, katie). husband(dwight, iva). husband(robert, kay). husband(pete, nancy).

> Things to query: mother(kay, nancy). mother(kay, kay). mother(kay, Who). press ;

wife $(X, Y)$ :- husband $(Y, X)$.
10 father $(X, Y)$ :- husband $(X, Z)$, mother $(Z, Y)$.

## Prolog

Inferencing process of Prolog. Example:
man(bob) query
Database includes rules:
father(bob).
man(X) :- father(X).
How does Prolog do it? Two possibilities:

1. Forward chaining: search for and find first proposition father(bob); goal is inferred by matching first proposition with right side of second rule father $(X)$ through instantiation of $X$ to bob, and then matching left side of second proposition to goal man(bob)

## Prolog

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Database includes rules:
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1. Forward chaining: search for and find first proposition father(bob); goal is inferred by matching first proposition with right side of second rule father $(X)$ through instantiation of $X$ to bob, and then matching left side of second proposition to goal man(bob)
2. Backward chaining: first match goal with left side of second proposition man(X) through the instantiation of $X$ to bob; as last step, match right side of second proposition (now father(bob)) with first proposition

Prolog uses Backward chaining. First match goal.

## Prolog

## Backtracking

- Multiple subgoals
- If fail to show proof of one subgoal, reconsider previous subgoal to find alternative solution (backtracking)
- Begin search where previous search left off
- Can take lots of time and space, because may find all possible proofs for every subgoal


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## Backtracking Example:

- Database has: male(mike) male(bob) parent(bob, shelley)
- Goal/query: male(X), parent(X, shelley)


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> Prolog finds first fact for subgoal male(X) and instantiates $X$ to mike; attempts to prove parent(mike, shelley) but fails
> Backtracks to first subgoal male(x); next finds male(bob) such that parent(bob, shelley) is true


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- Database has:
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> Backtracks to first subgoal male(x); next finds male(bob) such that parent(bob, shelley) is true
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> Note: could be more efficient here if reversed order of subgoals


## Prolog

## Simple arithmetic

- Prolog supports integer variables and arithmetic


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- Original Prolog had Scheme like + (7, X)
- Versions today use is operator


## Prolog

## Simple arithmetic

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Try in Prolog:
$A$ is $2+3$.
10 is $5+5$.
10 is $5+2$.
$A$ is $5 / 2$.

## Prolog

## Simple arithmetic

- Versions today use is operator

Try in Prolog:
?- $A$ is $2+3$.
$A=5$.
$A$ is $2+3$.
10 is $5+5$.
10 is $5+2$.
$A$ is $5 / 2$.
?- 10 is $5+5$. true.
?- 10 is $5+2$. false.
?- $5 / 2$ is 2.5 . false.
?- $A$ is $5 / 2$.
$\mathrm{A}=2.5$.

## Prolog

## Simple arithmetic

- All variables on the right must already be instantiated
- $A$ is $B / 17+C$. OK if $B$ and $C$ instantiated


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$>$ If Sum is not instantiated, then right side is not proper and cannot assign


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$>$ If Sum is instantiated, it is not proper in Prolog to set its left side!


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Simple arithmetic

- All variables on the right must already be instantiated
- $A$ is $B / 17+C$. OK if B and C instantiated
- Sum is Sum + 1
$>$ If Sum is not instantiated, then right side is not proper and cannot assign
$>$ If Sum is instantiated, it is not proper in Prolog to set its left side!
Not useful or legal in Prolog


## Prolog

Prolog example of numeric computation
Example: We know average speed of several automobiles on racetrack and the time on track. We can code relationship speed, time, distance

## Prolog

## Prolog example of numeric computation

```
speed.pl
speed(ford,100).
speed(chevy,105).
speed(dodge,95).
speed(volvo,80).
time(ford,20).
time(chevy,21).
time(dodge,24).
time(volvo,24).
distance(X,Y) :- speed(X,Speed),
    time(X,Time),
    Y is Speed * Time.
```


## Prolog

## Prolog example of numeric computation

```
speed.pl
speed(ford,100).
speed(chevy,105).
speed(dodge,95).
speed(volvo,80). Facts
time(ford,20).
time(chevy,21).
time(dodge,24).
time(volvo,24).
distance(X,Y) :- speed(X,Speed),
    time(X,Time),
    Y is Speed * Time.
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## Prolog example of numeric computation

```
speed.pl
speed(ford,100).
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time(ford,20).
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time(dodge,24).
time(volvo,24).
distance(X,Y) :- speed(X,Speed),
    time(X,Time),
    Y is Speed * Time.
```

Rule for getting distance: need to establish the Speed for given $X$ and the Time for given $X$, and then can set $Y$ to Speed * Time

## Prolog

## Prolog example of numeric computation



Try the queries:
time (chevy, X ).
distance(chevy,X).
distance(X,Y). (with ;)

## Prolog

## Prolog example of numeric computation



Try the queries:
time(chevy, $X$ ). Returns 21 distance(chevy,X).
Returns 2205 (105*21)
distance(X,Y). (with ;)
Returns all distances

## Prolog

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We will look at this more in our Prolog example in a moment

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Prolog's tracing model describes execution as 4 possible events:

1. call, which occurs at beginning of attempt to satisfy a goal
2. exit, when goal is satisfied
3. redo, when backtrack causes attempt to resatisfy goal
4. fail, when goal fails

## Prolog

## trace for our example


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## trace for our example


$>$ If distance is thought of as a subprogram, then call and exit can be related to execution models of imperative languages
> Other two events, redo and fail are unique to logical languages

## Prolog

## trace for our example

time(volvo,24).
distance(X,Y) :- speed(X,Speed),
time ( X, Time),
$Y$ is Speed * Time.

## Let's try it; type in Prolog compiler:

trace.
distance(chevy,X).

## Prolog

## trace for our example

[trace] ?- distance(chevy,X).<br>Call: (6) distance(chevy, _G1097) ?<br>Call: (7) speed(chevy, _G1170) ?<br>Exit: (7) speed(chevy, 105) ?<br>Call: (7) time(chevy, _G1170) ?<br>Exit: (7) time(chevy, 21) ?<br>Call: (7) _G1097 is 105*21 ?<br>Exit: (7) 2205 is $105 * 21$ ?<br>Exit: (6) distance(chevy, 2205) ?<br>X $=2205$.

## Prolog

## trace for our example

[trace] ?- distance(chevy,X).<br>Call: (6) distance(chevy, _G1097) ?<br>Depth of Internal variable to<br>matching<br>Process. In<br>textbook starts from 1 but not in practice

Let's unpack this

## Prolog

## trace for our example distance $(X, Y)$ :- speed $(X$, Speed $)$, time ( X, Time), $Y$ is Speed * Time.

[trace] ?- distance(chevy,X).<br>Call: (6) distance(chevy, _G1097) ?<br>Call: (7) speed(chevy, _G1170) ?<br>Depth<br>Internal variables to store instantiated value

## Prolog

## trace for our example

distance(X,Y) :- speed(X,Speed), time ( X ,Time),<br>$Y$ is Speed * Time.

[trace] ?- distance(chevy,X).
Call: (6) distance(chevy, _G1097) ?
Call: (7) speed(chevy, _G1170) ?
Exit: (7) speed(chevy, 105) ?

## Prolog

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distance( $\mathrm{X}, \mathrm{Y}$ ) :- speed(X,Speed), time ( X ,Time),<br>$Y$ is Speed * Time.

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## Prolog

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Let's unpack this

## Prolog

## trace for our example

distance( $\mathrm{X}, \mathrm{Y}$ ) :- speed(X,Speed), time ( X ,Time),<br>$Y$ is Speed * Time.

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## trace for our example

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[trace] ?- distance(chevy,X).
Call: (6) distance(chevy, _G1097) ?
Call: (7) speed(chevy, _G1170) ?
Exit: (7) speed(chevy, 105) ?
Call: (7) time(chevy, _G1170) ?
Exit: (7) time(chevy, 21) ?
Call: (7) _G1097 is $105 * 21$ ?
Exit: (7) 2205 is $105 * 21$ ?

## Prolog

## trace for our example

distance(X,Y) :- speed(X,Speed), time ( X, Time),<br>$Y$ is Speed * Time.

[trace] ?- distance(chevy,X).<br>Call: (6) distance(chevy, _G1097) ?<br>Call: (7) speed(chevy, _G1170) ?<br>Exit: (7) speed(chevy, 105) ?<br>Call: (7) time(chevy, _G1170) ?<br>Exit: (7) time(chevy, 21) ?<br>Call: (7) _G1097 is $105^{*} 21$ ?<br>Exit: (7) 2205 is $105 * 21$ ?<br>Exit: (6) distance(chevy, 2205) ?<br>X $=2205$.

## Prolog

## Another example

\% ['likes.pl'].
\% Based on sebesta book
\% control d, to exit
likes(jake,chocolate).
likes(jake,apricots).
likes(jake,bananas).
likes(darcie,licorice).
likes(darcie,apricots).
likes(darcie,bananas).
In compiler type:
['likes.pl'].
likes(jake,X), likes(darcie,X). Returns?

## Prolog

## Another example

In compiler type:
['likes.pl'].
likes(jake,X), likes(darcie,X).

Call: (7) likes(jake, _G1097) ? creep
Exit: (7) likes(jake, chocolate) ? creep
Call: (7) likes(darcie, chocolate) ? creep
Fail: (7) likes(darcie, chocolate) ? creep
Redo: (7) likes(jake, _G1097) ? creep
Exit: (7) likes(jake, apricots) ? creep
Call: (7) likes(darcie, apricots) ? creep
Exit: (7) likes(darcie, apricots) ? creep
X = apricots ;

## Prolog

## Another example

In compiler type:
['likes.pl'].
likes(jake,X), likes(darcie,X).
(after ;)

$$
\begin{aligned}
& \text { X = apricots ; } \\
& \text { Redo: (7) likes_darcie, apricots) ? creep } \\
& \text { Fail: (7) likes(darcie, apricots) ? creep } \\
& \text { Redo: (7) likes(jake,_G1097) ? creep } \\
& \text { Exit: (7) likes(jake, bananas) ? creep } \\
& \text { Call: (7) likes(darcie, bananas) ? creep } \\
& \text { Exit: (7) likes(darcie, bananas) ? creep } \\
& \text { X = bananas. }
\end{aligned}
$$

## Prolog

Control flow model for likes(jake,X), likes(darcie,X)


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- Can enter goal through call (forward) or redo (backward)
- Can exit through fail or exit


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Control flow model for likes(jake,X), likes(darcie,X)


- Four parts for each subgoal
- Can enter goal through call (forward) or redo (backward)
- Can exit through fail or exit
- Here second subgoal fails the first time, forcing return through redo to first subgoal


## Prolog

## List structure

- Prolog uses syntax of ML and Haskell to specify lists
- Example: [apple, prune, grape, kumquat]
[ ] empty list


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denotes a list with head $x$ and tail $y$


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## Prolog

## List structure

- Prolog uses syntax of ML and Haskell to specify lists
- Example: [apple, prune, grape, kumquat] [ ] empty list
- Prolog also has head and tail:
[x|y]
denotes a list with head $x$ and tail $y$
- Similar to? Most similar to Haskell (x : y) and ML (x :: y) format. Also conceptually related to car, cdr of Scheme.


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- This states that the constant list [apple, prune, grape, kumquat] is a new element of the relation name new_list (a name we just made up).


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- This states that the constant list [apple, prune, grape, kumquat] is a new element of the relation name new_list (a name we just made up).
- Does a similar thing to male(jake) ... It states that [apple, prune, grape, kumquat] is a new element of new_list


## Prolog

## List structure

- Lists can be created by a proposition: new_list([apple, prune, grape, kumquat]).
- This states that the constant list [apple, prune, grape, kumquat] is a new element of the relation name new_list (a name we just made up).
- Does a similar thing to male(jake) ... It states that [apple, prune, grape, kumquat] is a new element of new_list
- So we can also have a second statement new_list([apricot, peach, pear)].


## Prolog

lists_simple.pl
new_list([apple,prune,grape,kumquot]). new_list([apricot,peach,pear]).

## Prolog

lists_simple.pl
new_list([apple,prune,grape,kumquot]). new_list([apricot,peach,pear]).

Run in compiler:
new_list $(X)$.
new_list([X|Y]).
use ; after entering.
Returns?

## Prolog

lists_simple.pl
new_list([apple,prune,grape,kumquot]). new_list([apricot,peach,pear]).

## Run in compiler:

new_list $(X)$.
?- new_list(X).
X = [apple, prune, grape, kumquot] ;
X = [apricot, peach, pear].

## Prolog

lists_simple.pl
new_list([apple,prune,grape,kumquot]). new_list([apricot,peach,pear]).

Run in compiler:
new_list([X|Y]).
?- new_list([X|Y]).
X = apple,
Y = [prune, grape, kumquot] ;
X = apricot,
${ }^{76} \mathrm{Y}=$ [peach, pear].

Returns the head and tail of each list!

## Prolog

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- But we can also construct: [pickle, [peanut, prune, popcorn]]
creates [pickle, peanut, prune, popcorn]


## Prolog

- The | notation can both dismantle and construct lists
- We saw dismantling into a head and tail
- But we can also construct: [pickle, [peanut, prune, popcorn]]
creates [pickle, peanut, prune, popcorn]
These are all equivalent!

[apricot, peach, pear | []]
[apricot, peach | [pear] ]
79 [apricot | [peach, pear] ]


## Prolog

- File lists_simple4.pl
\% run in compiler:
\% new_list(X).
\% use ; after entering.
new_list([apricot,peach,pear | []]). new_list([apricot,peach | [pear]]). new_list([apricot | [peach,pear]]).


## Prolog

- File lists_simple4.pl
\% run in compiler:
\% new_list(X).
\% use ; after entering.
new_list([apricot,peach,pear | []]). new_list([apricot,peach | [pear]]). new_list([apricot | [peach,pear]]).

In compiler:
?- new_list(X).
X = [apricot, peach, pear] ;
X = [apricot, peach, pear] ;
${ }_{\text {s }} X=$ [apricot, peach, pear].

## Prolog

- File lists_simple4.pl
\% run in compiler:
\% new_list(X).
\% use ; after entering.
new_list([apricot,peach,pear | []]). new_list([apricot,peach | [pear]]). new_list([apricot | [peach,pear]]).

In compiler:
?- new_list(X).
X = [apricot, peach, pear] ;
X = [apricot, peach, pear] ;
${ }_{82} X=$ [apricot, peach, pear].

## Prolog

- File lists_simple2.pl
new_list([H|T], H, T).

What does this do??

## Prolog

- File lists_simple2.pl
new_list([H|T], H, T).

What does this do??
?- new_list([apple,prune,grape,kumquot],X,Y).
X = apple,
$Y=$ [prune, grape, kumquot].
Returns head and tail

## Prolog

- File lists_simple2.pl
new_list([H|T], H, T).

What does this do??
?- new_list(X,apple,[prune, grape, kumquot]). X = [apple, prune, grape, kumquot].

Constructs list

## Prolog

- File lists_simple2.pl
new_list([H|T], H, T).

What does this do??
?- new_list([apple,prune,grape,kumquot],X,Y).
X = apple,
$Y=$ [prune, grape, kumquot]. Returns head and tail
?- new_list(X,apple,[prune, grape, kumquot]). X = [apple, prune, grape, kumquot].

Constructs list

## Prolog

- File lists_simple2.pl
new_list([H|T], H, T).
?- new_list([apple,prune,grape,kumquot],prune, [prune, grape, kumquot]).

Returns??

## Prolog

- File lists_simple2.pl
new_list([H|T], H, T).
?- new_list([apple,prune,grape,kumquot],prune, [prune, grape, kumquot]).

Returns?? false.

