Reinforcement Learning Lab

Odelia Schwartz,
Luis Gonzalo Sánchez Giraldo

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Rescorla-Wagner rule (1972)

- Minimize difference between received reward and predicted reward

- Binary variable u (1 if stimulus is present; 0 if absent)

- Predicted reward v

- Linear weight w

$$v = wu$$

- If stimulus u is present:

$$v = w$$

based on Dayan and Abbott book

Rescorla-Wagner rule (1972)

- Minimize squared error between received reward r and predicted reward v:

$$(r - v)^2$$
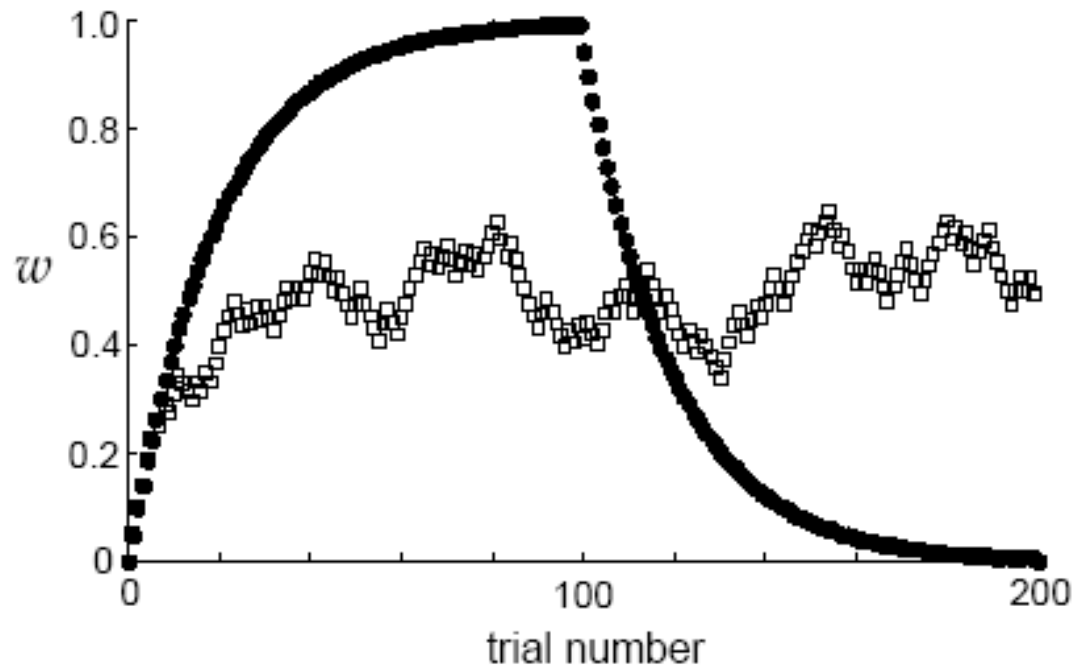
(average over presentations of stimulus and reward)

- Update weight:

$$w \rightarrow w + \varepsilon(r - v)u$$

ε learning rate

Also known as delta learning rule: $\delta = r - v$

Acquisition and extinction

- Solid: First 100 trials: reward (r=1) paired with stimulus; next 100 trials no reward (r=0) paired with stimulus (learning rate .05)
- Dashed: Reward paired with stimulus randomly 50 percent of time

From Dayan and Abbott book

Temporal Difference Learning

Want $$v_t = r_t + \boxed{r_{t+1} + r_{t+2} + r_{t+3} \dots}$$

(here t represents time within a trial; reward can come at any time within a trial. Sutton and Barto interpret v_t as the prediction of total future reward expected from time t onward until the end of the trial)

Based on Dayan slides; Daw slides

Temporal Difference Learning

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Prediction error:

$$\delta_t = (r_t + r_{t+1} + r_{t+2} + r_{t+3} \ldots) - V_t$$

Temporal Difference Learning

Want $\quad v_t = r_t + \boxed{r_{t+1} + r_{t+2} + r_{t+3}\dots}$

(here t represents time within a trial)

But we don't want to wait forever for all future rewards…

$$r_{t+1}; r_{t+2}; r_{t+3}\dots$$

Temporal Difference Learning

Want $v_t = r_t + r_{t+1} + r_{t+2} + r_{t+3}....$

(here t represents time within a trial)

Recursion "trick": $v_t = r_t + v_{t+1}$

Based on Dayan slides; Daw slides

Temporal Difference Learning

From recursion want:

$$v_t = r_t + v_{t+1}$$

Error:

$$\delta_t = r_t + v_{t+1} - v_t$$

Temporal Difference Learning

From recursion want:

$$v_t = r_t + v_{t+1}$$

Error:

$$\delta_t = r_t + v_{t+1} - v_t$$

Update:

$$v_t \rightarrow v_t + \varepsilon(r_t + v_{t+1} - v_t)$$

$$= (1 - \varepsilon)v_t + \varepsilon(r_t + v_{t+1})$$

RV versus TD
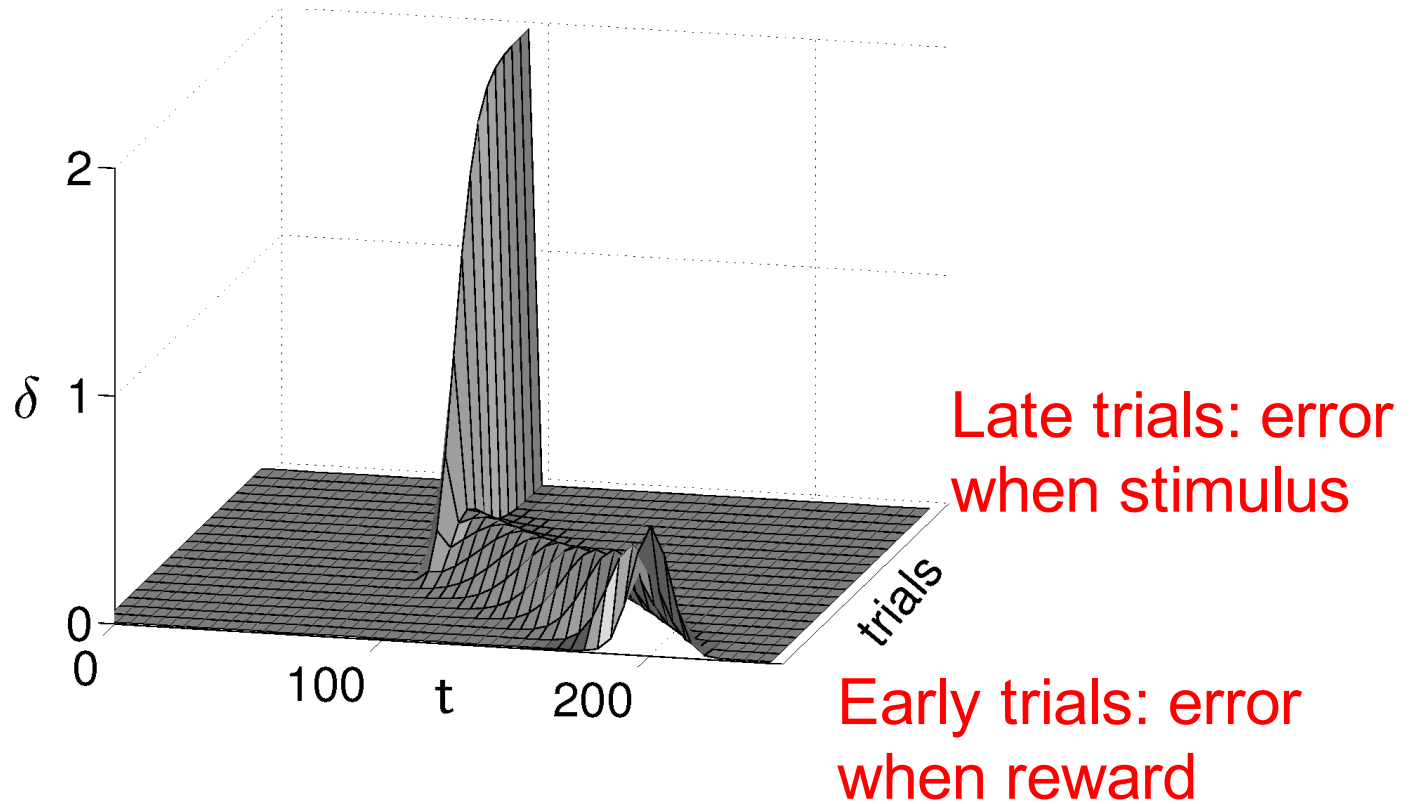
- Rescorla-Wagner error: (n represents trial)

$$\delta_n = r_n - v_n$$

- Temporal Difference Error: (t is time within a trial)

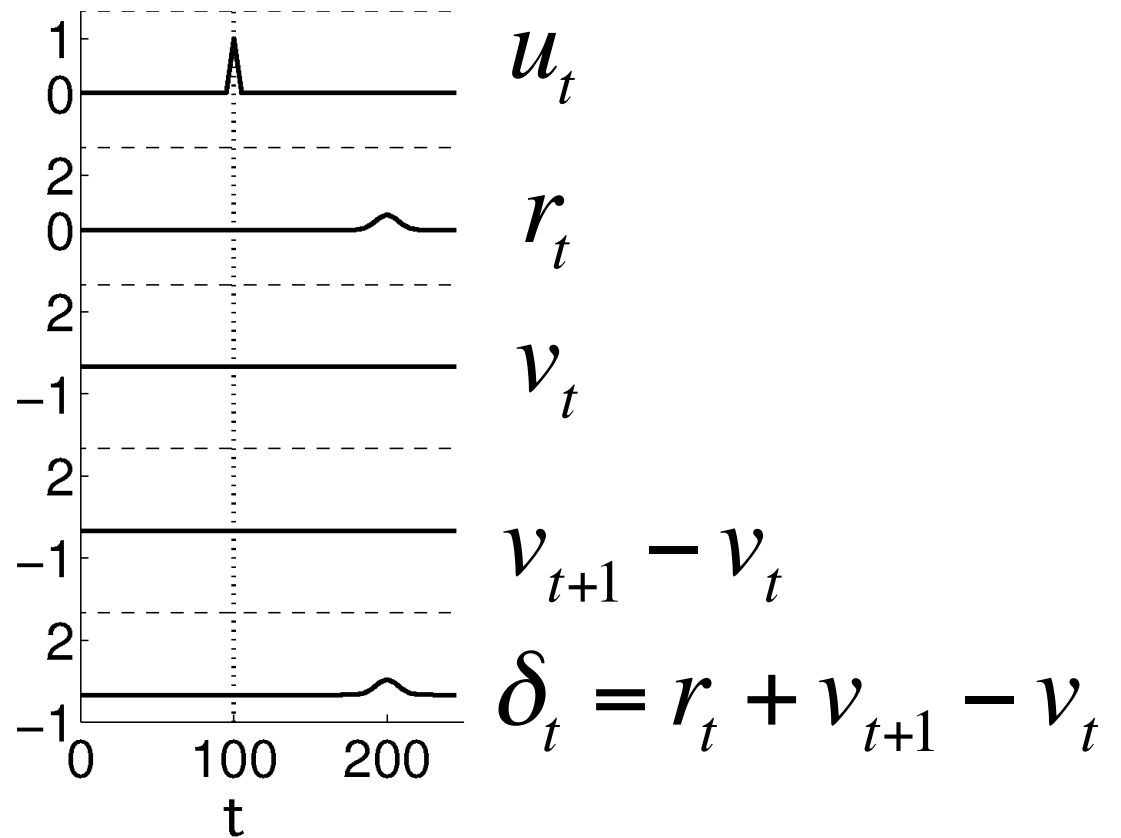$$\delta_t = r_t + v_{t+1} - v_t$$

Updates are causal

Temporal Difference Learning

Late trials: error when stimulus

Early trials: error when reward

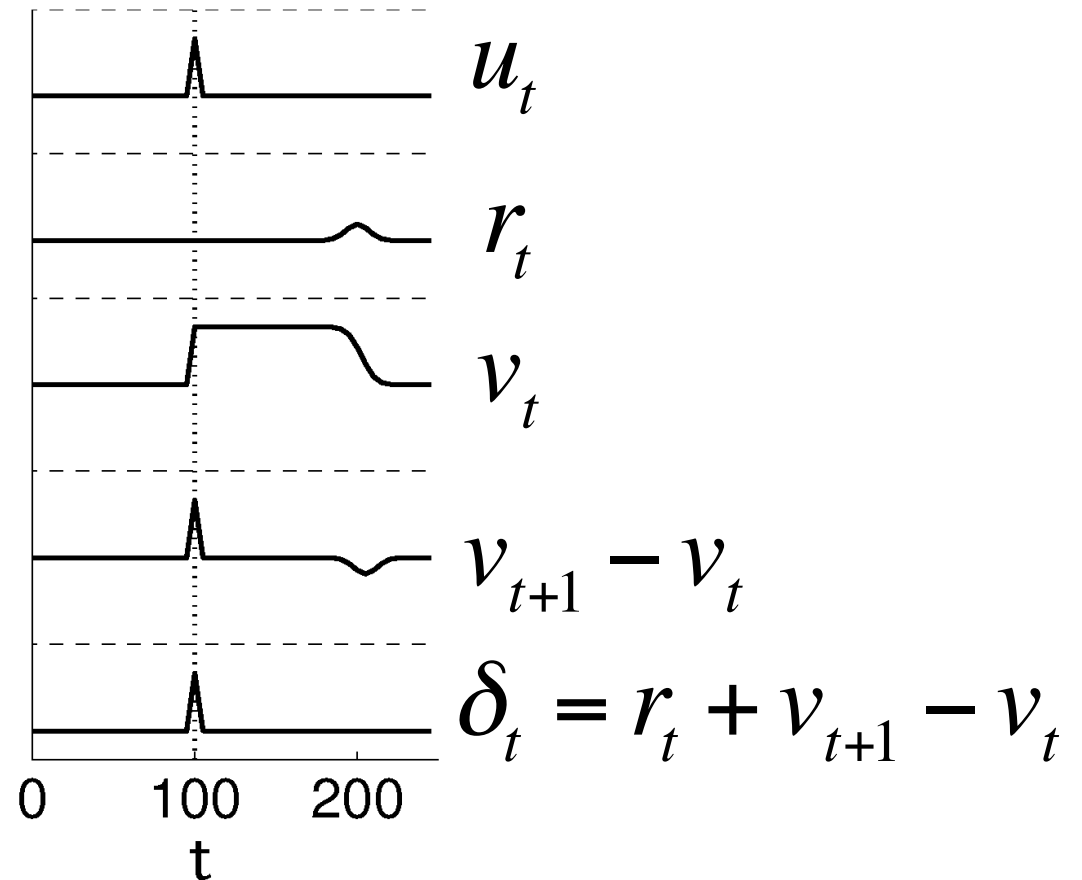Dayan and Abbott Book: Surface plot of prediction error (stimulus at 100; reward at 200)
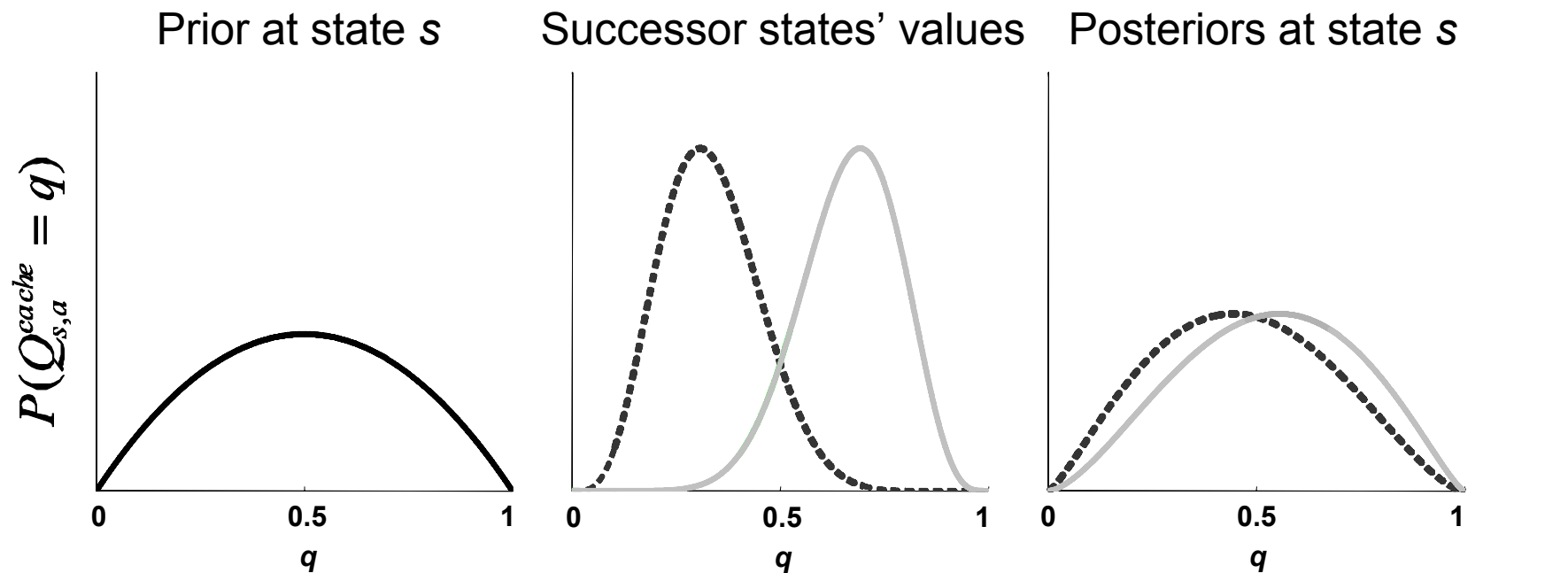
Temporal Difference Learning

Before learning

Temporal Difference Learning

Whole distribution: Daw et al. 2015 paper

Prior at state s	Successor states' values	Posteriors at state s

$P(Q_{s,a}^{cache} = q)$

0   0.5   1
q

0   0.5   1
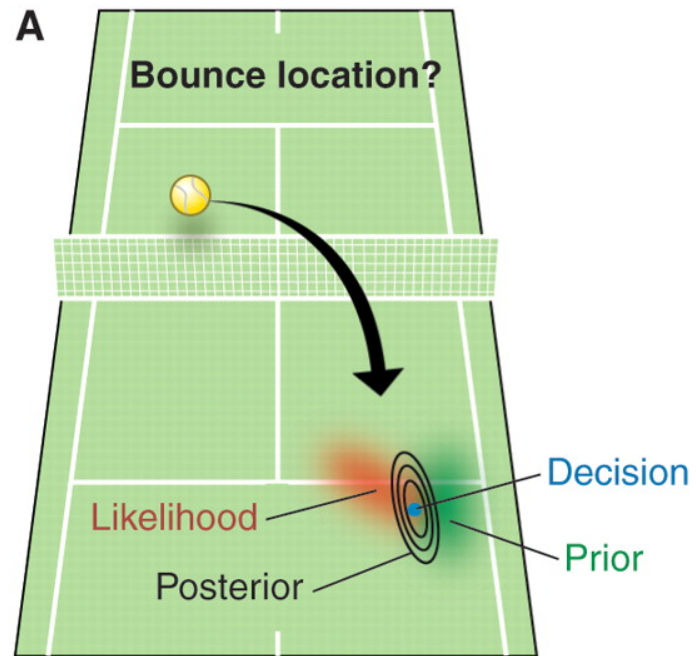q

0   0.5   1
q

Two example
Successors – more
and less favorable

Prior nudged in direction
of each successor

Learning both a mean and a variance: uses Beta distribution

Bayesian inference

Koerding 2007